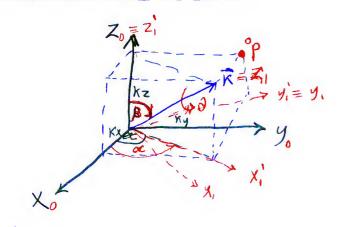
Axis/Angle representation



K unit vector

- ويمكن تهنياه بمركبتين فقط ومنها نستنتج المركبة الثالثة - و يمكن تمثيل الدوراك في الفراخ من خلال من الفراخ من خلال عن الفراخ من خلال من الموراك حولا في الموراك حولا في المراكبة الموراك حولا في المراكبة الموراك حولا في المراكبة المراكبة

P: to be Rotated about K axis

+ Assume Frame of Early frame Contain R] frame I will be well the contain R]

→ Assume Frame 1 Attached to K

K in the direction of 2,

given : °p -ip

 ${}^{1}P_{hoffre} {}^{1}R_{0} {}^{\circ}P = ({}^{\circ}R_{1})^{-1} {}^{\circ}P_{hoffare}$ ${}^{1}P_{new} = R(z, \theta) {}^{1}P_{hoffare}$ $= R(z, \theta) ({}^{\circ}R_{1})^{-1} {}^{\circ}P_{hoffare}$

Pnew = Pnew Pnew

Pnew = ${}^{\circ}R$, $R(2,\theta)(R_1)^{\circ}$ P before

Lisimilarly Transformation $R = {}^{\circ}R$, $R(2,\theta)$ $({}^{\circ}R_1)^{-1}$ Robotion two of the Gafel

fromo line frame the curboll

 ${}^{\circ}R_{1} = R(z, \alpha) R(y, \beta) \leftarrow$ $(R_{1}R_{2})^{-1} = R_{2}^{-1} R_{1}^{-1}$ $({}^{\circ}R_{1})^{-1} = R(y, \beta) R^{-1}(z, \alpha)$ $= R(y, -\beta) R(z, -\alpha) \leftarrow$

 $R = R(z, \alpha) R(y, \beta) R(z, \theta) R(y, -\beta)$ $R(z, -\alpha)$

 $ton \alpha = \frac{\kappa_y}{\kappa_\chi} \rightarrow \alpha$ $ton \beta = \frac{\sqrt{\kappa_x^2 + \kappa_y^2}}{\kappa_z} \rightarrow \beta$

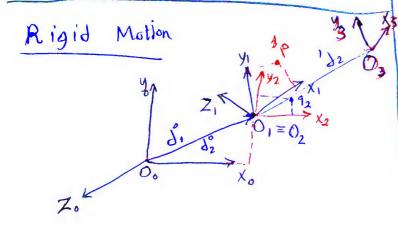
given: $\vec{R} = (K_X, K_Y, K_Z)$ and θ we can find the rotation $\wedge - \wedge$

$$R = \begin{bmatrix} \kappa_{x}^{2} (1-C_{\theta}) + C_{\theta} & - & - \\ - & \kappa_{y}^{2} (1-C_{\theta}) + C_{\theta} & - \\ - & - & \kappa_{z}^{2} (1-C_{\theta}) + C_{\theta} \end{bmatrix}$$

$$V_{11} + V_{2,2} + V_{3,3} = 1 - C_{\theta} + 3C_{\theta}$$

$$= 1 + 2C_{\theta}$$

$$C_{\theta} = \frac{Y_{11} + Y_{2,2} + Y_{3,-1}}{2}$$



Frame 1 with respect to Frame o

- 1- Translation T(a, b, c)
- 2- Rotation R (<, B, 8)

given 40 regular op

$$^{\circ}9 = d_2 + ^{\circ}9 \quad (Right \ V)$$

$${}^{\circ}P = {}^{\circ}d_{1} + {}^{2}P$$

$$= {}^{\circ}d_{1} + {}^{2}R_{1}{}^{!}P$$

$$= {}^{\circ}d_{1} + {}^{\circ}R_{1}{}^{!}P$$

1- distance between 0, and 00 With respect to frame 1
2- Orientation of frame 1 with respect to frame 0 0 R.

H: homogenous Transformation Matrix

$$\begin{bmatrix} P \\ 1 \end{bmatrix} = \begin{bmatrix} P \\ 0 \\ 1 \end{bmatrix} \begin{bmatrix} P \\ 1 \end{bmatrix} \begin{bmatrix} P \\ 1 \end{bmatrix} \begin{bmatrix} P \\ 1 \end{bmatrix}$$

$$H_{3} = {}^{\circ}H_{1} H_{3}$$

$$= \begin{bmatrix} {}^{\circ}R_{1} & {}^{\circ}d_{1} \end{bmatrix} \begin{bmatrix} {}^{\prime}R_{3} & {}^{\prime}d_{3} \end{bmatrix}$$

$$= \begin{bmatrix} {}^{\circ}R_{3} & {}^{\circ}R_{1} d_{3} + {}^{\circ}d_{1} \end{bmatrix}$$

$$H^{-1} \neq H^{T}$$

$$H^{-1} = \begin{bmatrix} R^{T} & -R^{T} J \end{bmatrix}$$